Identify the domain and range of each function.

1. $f(x)=\sqrt{4 x}$

## ANSWER:

$\mathrm{D}=\{x \mid x \geq 0\} ; \mathrm{R}=\{f(x) \mid f(x) \geq 0\}$
2. $f(x)=\sqrt{x-5}$

## ANSWER:

$\mathrm{D}=\{x \mid x \geq 5\} ; \mathrm{R}=\{f(x) \mid f(x) \geq 0\}$
3. $f(x)=\sqrt{x+8}-2$

ANSWER:
$\mathrm{D}=\{x \mid x \geq-8\} ; \mathrm{R}=\{f(x) \mid f(x) \geq-2\}$

Graph each function. State the domain and range.
4. $f(x)=\sqrt{x}-2$

ANSWER:
$\mathrm{D}=\{x \mid x \geq 0\} ; \mathrm{R}=\{f(x) \mid f(x) \geq-2\}$

5. $f(x)=3 \sqrt{x-1}$

ANSWER:
$\mathrm{D}=\{x \mid x \geq 1\} ; \mathrm{R}=\{f(x) \mid f(x) \geq 0\}$

6. $f(x)=\frac{1}{2} \sqrt{x+4}-1$

ANSWER:
$\mathrm{D}=\{x \mid x \geq-4\} ; \mathrm{R}=\{f(x) \mid f(x) \geq-1\}$

7. $f(x)=-\sqrt{3 x-5}+5$

ANSWER:
$\mathrm{D}=\left\{x \left\lvert\, x \geq \frac{5}{3}\right.\right\} ; \mathrm{R}=\{f(x) \mid f(x) \leq 5\}$

8. OCEAN The speed that a tsunami, or tidal wave, can travel is modeled by the equation $v=356 \sqrt{d}$. where $v$ is the speed in kilometers per hour and $d$ is the average depth of the water in kilometers. A tsunami is found to be traveling at 145 kilometers per hour. What is the average depth of the water? Round to the nearest hundredth of a kilometer.

ANSWER:
0.17 km

## Graph each inequality.

9. $f(x) \geq \sqrt{x}+4$

ANSWER:

10. $f(x) \leq \sqrt{x-6}+2$

ANSWER:

11. $f(x)<-2 \sqrt{x+3}$

ANSWER:

12. $f(x)>\sqrt{2 x-1}-3$

ANSWER:


Identify the domain and range of each function.
13. $f(x)=-\sqrt{2 x}+2$

ANSWER:
$\mathrm{D}=\{x \mid x \geq 0\} ; \mathrm{R}=\{f(x) \mid f(x) \leq 2\}$
14. $f(x)=\sqrt{x}-6$

ANSWER:
$\mathrm{D}=\{x \mid x \geq 0\} ; \mathrm{R}=\{f(x) \mid f(x) \geq-6\}$
15. $f(x)=4 \sqrt{x-2}-8$

ANSWER:
$\mathrm{D}=\{x \mid x \geq 2\} ; \mathrm{R}=\{f(x) \mid f(x) \geq-8\}$
16. $f(x)=\sqrt{x+2}+5$

ANSWER:
$\mathrm{D}=\{x \mid x \geq-2\} ; \mathrm{R}=\{f(x) \mid f(x) \geq 5\}$
17. $f(x)=\sqrt{x-4}-6$

ANSWER:
$\mathrm{D}=\{x \mid x \geq 4\} ; \mathrm{R}=\{f(x) \mid f(x) \geq-6\}$
18. $f(x)=-\sqrt{x-6}+5$

ANSWER:
$\mathrm{D}=\{x \mid x \geq 6\} ; \mathrm{R}=\{f(x) \mid f(x) \leq 5\}$

Graph each function. State the domain and range.
19. $f(x)=\sqrt{6 x}$

ANSWER:

$\mathrm{D}=\{x \mid x \geq 0\} ; \mathrm{R}=\{f(x) \mid f(x) \geq 0\}$
20. $f(x)=-\sqrt{5 x}$

ANSWER:

$\mathrm{D}=\{x \mid x \geq 0\} ; \mathrm{R}=\{f(x) \mid f(x) \leq 0\}$
21. $f(x)=\sqrt{x-8}$

ANSWER:

$\mathrm{D}=\{x \mid x \geq 8\} ; \mathrm{R}=\{f(x) \mid f(x) \geq 0\}$
22. $f(x)=\sqrt{x+1}$

ANSWER:

$\mathrm{D}=\{x \mid x \geq-1\} ; \mathrm{R}=\{f(x) \mid f(x) \geq 0\}$
23. $f(x)=\sqrt{x+3}+2$

24. $f(x)=\sqrt{x-4}-10$

## ANSWER:


$\mathrm{D}=\{x \mid x \geq 4\} \mathrm{R}=\{f(x) \mid f(x) \geq-10\}$
25. $f(x)=2 \sqrt{x-5}-6$

ANSWER:

$\mathrm{D}=\{x \mid x \geq 5\} \mathrm{R}=\{f(x) \mid f(x) \geq-6\}$
26. $f(x)=\frac{3}{4} \sqrt{x+12}+3$

ANSWER:

$\mathrm{D}=\{x \mid x \geq-12\} \mathrm{R}=\{f(x) \mid f(x) \geq 3\}$
27. $f(x)=-\frac{1}{5} \sqrt{x-1}-4$

ANSWER:

$\mathrm{D}=\{x \mid x \geq 1\} \mathrm{R}=\{f(x) \mid f(x) \leq-4\}$
28. $f(x)=-3 \sqrt{x+7}+9$

ANSWER:

$\mathrm{D}=\{x \mid x \geq-7\} \mathrm{R}=\{f(x) \mid f(x) \leq 9\}$
29. SKYDIVING The approximate time $t$ in seconds that it takes an object to fall a distance of $d$ feet is given by $t=\sqrt{\frac{d}{16}}$. Suppose a parachutist falls 11 seconds before the parachute opens. How far does the parachutist fall during this time?
30. CCSS MODELING The velocity of a roller coaster as it moves down a hill is $V=\sqrt{v^{2}+64 h}$, where $v$ is the initial velocity in feet per second and $h$ is the vertical drop in feet. The designer wants the coaster to have a velocity of 90 feet per second when it reaches the bottom of the hill.
a. If the initial velocity of the coaster at the top of the hill is 10 feet per second, write an equation that models the situation.
b. How high should the designer make the hill?

ANSWER:
a. $90=\sqrt{100+64 h}$
b. 125 ft

## Graph each inequality.

31. $y<\sqrt{x-5}$

ANSWER:


ANSWER:
1936 ft
32. $y>\sqrt{x+6}$

ANSWER:

33. $y \geq-4 \sqrt{x+3}$

ANSWER:

34. $y \leq-2 \sqrt{x-6}$

ANSWER:

35. $y>2 \sqrt{x+7}-5$

ANSWER:

36. $y \geq 4 \sqrt{x-2}-12$

ANSWER:

37. $y \leq 6-3 \sqrt{x-4}$

ANSWER:

38. $y<\sqrt{4 x-12}+8$

ANSWER:

39. PHYSICS The kinetic energy of an object is the energy produced due to its motion and mass. The formula for kinetic energy, measured in joules $j$, is $E$ $=0.5 m v^{2}$, where $m$ is the mass in kilograms and $v$ is the velocity of the object in meters per second.
a. Solve the above formula for $v$.
b. If a 1500 -kilogram vehicle is generating 1 million joules of kinetic energy, how fast is it traveling?
c. Escape velocity is the minimum velocity at which an object must travel to escape the gravitational field of a planet or other object.

Suppose a 100, 000-kilogram ship must have a kinetic energy of $3.624 \times 10^{14}$ joules to escape the gravitational field of Jupiter. Estimate the escape velocity of Jupiter.

ANSWER:
a. $v=\sqrt{\frac{2 E}{m}}$
b. about $36.5 \mathrm{~m} / \mathrm{s}$
c. about $85,135 \mathrm{~m} / \mathrm{s}$
40. CCSS REASONING After an accident, police can determine how fast a car was traveling before the driver put on his or her brakes by using the equation $v=\sqrt{30 \mathrm{fd}}$. In this equation, $v$ represents the speed in miles per hour, $f$ represents the coefficient of friction, and $d$ represents the length of the skid marks in feet. The coefficient of friction varies depending on road conditions. Assume that $f=$ 0.6 .
a. Find the speed of a car that skids 25 feet.
b. If your car is going 35 miles per hour, how many feet would it take you to stop?
c. If the speed of a car is doubled, will the skid be twice as long? Explain.
ANSWER:
a. about 21.2 mph
b. about 68 ft
c. No; it is not a linear function. The skid will be 4 times as long.

Write the square root function represented by each graph.
41.


## ANSWER:

$y=\sqrt{x-4}-6$
42.


ANSWER:
$y=\sqrt{x+2}+4$
43.


ANSWER:
$y=-\sqrt{x+6}-6$
44. MULTIPLE REPRESENTATIONS In this problem, you will use the following functions to investigate transformations of square root functions.

$$
f(x)=4 \sqrt{x-6}+3 \quad h(x)=\sqrt{16 x+1}-6 \quad h(x)=\sqrt{x+3}+2
$$

a. GRAPHICAL Graph each function on the same set of axes.
b. ANALYTICAL Identify the transformation on the graph of the parent function. What values caused each transformation?
c. ANALYTICAL Which functions appear to be stretched or compressed vertically? Explain your reasoning.
d. VERBAL The two functions that are stretched appear to be stretched by the same magnitude. How is this possible?
e. TABULAR Make a table of the rate of change for all three functions between 8 and 12 as compared to 12 and 16 . What generalization about rate of change in square root functions can be made as a result of your findings?
ANSWER:
a.

b. $f(x)$ : 6 units to the right, 3 units up; $g(x): \frac{1}{16}$ to the left, 6 units down; $h(x): 3$ units to the left, 2 units up
c. Sample answer: $f(x)$ and $g(x)$ appear to be stretched because the graph increases much more quickly than the parent graph.
d. Sample answer: They are stretched by the same magnitude because $4=\sqrt{16}$.
e.

| $x=8$ | $x=12$ | $x=16$ | Rate of <br> Change <br> between 8 <br> and 12 | Rate of <br> Change <br> between 12 <br> and 16 |
| :---: | :---: | :---: | :---: | :---: |
| $f(8)=8.66$ | $f(12)=12.798$ | $f(16)=15.65$ | 1.0345 | 0.713 |
| $g(8)=5.36$ | $g(12)=7.89$ | $g(16)=10.03$ | 0.6325 | 0.535 |
| $h(8)=5.317$ | $h(12)=5.873$ | $h(16)=6.359$ | 0.139 | 0.1215 |

The rate of change decreases as the $x$-values increase for square root functions of the form $a \sqrt{x-b}+c$, where $a>0$.
45. PENDULUMS The period of a pendulum can be represented by $T=2 \pi \sqrt{\frac{L}{g}}$, where $T$ is the time in seconds, $L$ is the length in feet, and $g$ is gravity, 32 feet per second squared.
a. Graph the function for $0 \leq L \leq 10$.
b. What is the period for lengths of 2,5 , and 8 feet?


ANSWER:
a.

b. $1.57 \mathrm{~s}, 2.48 \mathrm{~s}, 3.14 \mathrm{~s}$
46. PHYSICS Using the function $m=\frac{m_{0}}{\sqrt{1-\left(\frac{v^{2}}{c^{2}}\right)}}$,

Einstein's theory of relativity states that the apparent mass $m$ of a particle depends on its velocity $v$. An object that is traveling extremely fast, close to the speed of light $c$, will appear to have more mass compared to its mass at rest, $m_{0}$.
a. Use a graphing calculator to graph the function for a 10,000 -kilogram ship for the domain $0 \leq v \leq 300,000,000$. Use 300 million meters per second for the speed of light.
b. What viewing window did you use to view the graph?
c. Determine the apparent mass $m$ of the ship for speeds of 100 million, 200 million, and 299 million meters per second.

ANSWER:
a.

b. $\{0,400,000,000\}$ scl: $50,000,000$ by $\{0,100,000\}$ scl: 20,000
c. (100 million, 10,607 )(200 million, 13,416 )(299
million, 122,577 )
47. CHALLENGE Write an equation for a square root function with a domain of $\{x \mid x \geq-4\}$, a range of $\{y \mid y \leq 6\}$, and that passes through $(5,3)$.

ANSWER:
Sample answer: $y=-\sqrt{x+4}+6$
48. REASONING For what positive values of $a$ are the domain and range of $f(x)=\sqrt[a]{x}$ the set of real numbers?

## ANSWER:

all positive odd numbers
49. OPEN ENDED Write a square root function for which the domain is $\{x \mid x \geq 8\}$ and the range is $\{y \mid y \leq 14\}$.

## ANSWER:

Sample answer : $y=-\sqrt{x-8}+14$
50. WRITING IN MATH Explain why there are limitations on the domain and range of square root functions.

## ANSWER:

Sample answer: The domain is limited because square roots of negative numbers are imaginary. The range is limited due to the limitation of the domain.
51. CCSS CRITIQUE Cleveland thinks that the graph and the equation represent the same function. Molly disagrees. Who is correct? Explain your reasoning.


$$
y=\sqrt{5 x+10}
$$

## ANSWER:

Molly; $y=\sqrt{5 x+10}$ has an $x$-intercept of -2 and would be to the right of the given graph.
52. WRITING IN MATH Explain why $y= \pm \sqrt{x}$ is not a function.

ANSWER:
To be a function, for every $x$-value there must be exactly one $y$-value. For every $x$ in this equation there are two $y$-values, one that is negative and one that is positive. Also, the graph of $y= \pm \sqrt{x}$ does not pass the vertical line test.
53. OPEN ENDED Write an equation of a relation that contains a radical and its inverse such that:
a. the original relation is a function, and its inverse is not a function
b. the original relation is not a function, and its inverse is a function.

## ANSWER:

a. Sample answer: The original is $y=x^{2}+2$ and inverse is $y= \pm \sqrt{x-2}$.
b. Sample answer: The original is $y= \pm \sqrt{x}+4$ and inverse is $y=(x-4)^{2}$.
54. The expression $\frac{-64 x^{6}}{8 x^{3}}, x \neq 0$, is equivalent to

A $8 x^{2}$
B $8 x^{3}$
C $-8 x^{2}$
D $-8 x^{3}$

ANSWER:
D
55. PROBABILITY For a game, Patricia must roll a standard die and draw a card from a deck of 26 cards, each card having a letter of the alphabet on it. What is the probability that Patricia will roll an odd number and draw a letter in her name?

F $\frac{2}{3}$
G $\frac{3}{26}$
H $\frac{1}{13}$

J $\frac{1}{26}$

ANSWER:
G
56. SHORT RESPONSE What is the product of $(d+$
$6)$ and $(d-3)$ ?

ANSWER:
$d^{2}+3 d-18$
57. SAT/ACT Given the graph of the square root function below, which must be true?
I. The domain is all real numbers.
II. The function is $y=\sqrt{x}+3.5$.
III. The range is about $\{y \mid y \geq 3.5\}$.


A I only
B I, II, and III
C II and III only
D II only
E III only

ANSWER:
E

Determine whether each pair of functions are inverse functions. Write yes or no.
$f(x)=2 x$
58.
$g(x)=\frac{1}{2} x$
ANSWER:
Yes
$f(x)=3 x-7$
59.
$g(x)=\frac{1}{3} x-\frac{7}{16}$
ANSWER:
No
60.
$f(x)=\frac{3 x+2}{5}$
$g(x)=\frac{5 x-2}{3}$
ANSWER:
Yes
61. TIME The formula $h=\frac{m}{60}$ converts minutes $m$ to hours $h$, and $d=\frac{h}{24}$ converts hours $h$ to days $d$. Write a function that converts minutes to days.

## ANSWER:

$$
[d \circ h](m)=\frac{m}{1440}
$$

62. CABLE TV The number of households in the United States with cable TV after 1985 can be modeled by the function $C(t)=-43.2 t^{2}+1343 t+$ 790 , where $t$ represents the number of years since 1985.
a. Graph this equation for the years 1985 to 2005.
b. Describe the turning points of the graph and its end behavior.
c. What is the domain of the function? Use the graph to estimate the range for the function.
d. What trends in households with cable TV does the graph suggest? Is it reasonable to assume that the trend will continue indefinitely?

## ANSWER:

a.

b. rel. max. between $t=15$ and $t=16$, and no rel. min.; $C(t) \rightarrow-\infty$ as $t \rightarrow-\infty, C(t) \rightarrow-\infty$ as $t \rightarrow+\infty$
c. $\mathrm{D}=\{$ all real numbers $\} ; \mathrm{R}=\{y \mid y \leq 11,225\}$
d. The number of cable TV systems rose steadily from 1985 to 2000 . Then the number began to decline. The trend may continue for some years, but the number of cable TV systems cannot decline at this rate indefinitely. The number cannot fall below 0 . It is not likely that the number would come close to 0 for the foreseeable future; there is no reason to believe that cable TV systems will not be in use.

Determine whether each number is rational or irrational.
63.6 .34

ANSWER:
rational
64. 3.787887888...

ANSWER:
irrational
65. 5.333...

ANSWER:
rational
66. 1.25

ANSWER:
rational

