State whether each sentence is *true* or *false*. If *false*, replace the underlined term to make a true sentence.

1. The coefficient of the first term of a polynomial in standard form is called the <u>leading coefficient</u>.

ANSWER:

true

2. Polynomials that cannot be factored are called polynomials in one variable.

ANSWER:

false; prime polynomials

3. A <u>prime polynomial</u> has a degree that is one less than the original polynomial.

ANSWER:

false; depressed polynomial

4. A point on the graph of a function where no other nearby point has a greater *y*-coordinate is called a relative maximum.

ANSWER:

true

5. A <u>polynomial function</u> is a continuous function that can be described by a polynomial equation in one variable.

ANSWER:

true

6. To <u>simplify</u> an expression containing powers means to rewrite the expression without parentheses or negative exponents.

ANSWER:

true

7. <u>Synthetic division</u> is a shortcut method for dividing a polynomial by a binomial.

ANSWER:

true;

8. The relative maximum and relative minimum of a function are often referred to as <u>end behavior</u>.

ANSWER: false; turning points

9. When a polynomial is divided by one of its binomial factors, the quotient is called a <u>depressed polynomial</u>.

ANSWER:

true

10. $(x^3)^2 + 3x^3 - 8 = 0$ is a power function.

ANSWER:

false; written in quadratic form

Simplify. Assume that no variable equals 0.

11.
$$\frac{14x^{2}y}{2x^{3}y^{5}}$$
ANSWER:

$$\frac{7x}{y^4}$$

12. 3t(tn - 5)

ANSWER:
$$3t^2n - 15t$$

13. $(4r^2 + 3r - 1) - (3r^2 - 5r + 4)$ ANSWER: $r^2 + 8r - 5$ 14. $(x^4)^3$

15.
$$(m+p)(m^2 - 2mp + p^2)$$

ANSWER:

$$m^3 - m^2 p - mp^2 + p^3$$

16.
$$3b(2b - 1) + 2b(b + 3)$$

ANSWER:
 $8b^{2} + 3b$

Simplify.
17.
$$\frac{12x^{4}y^{5} + 8x^{3}y^{7} - 16x^{2}y^{6}}{4xy^{5}}$$
ANSWER:
 $3x^{3} + 2x^{2}y^{2} - 4xy$
18. $(6y^{3} + 13y^{2} - 10y - 24) \div (y + 2)$
ANSWER:
 $6y^{2} + y - 12$
19. $(a^{4} + 5a^{3} + 2a^{2} - 6a + 4)(a + 2)^{-1}$
ANSWER:
 $a^{3} + 3a^{2} - 4a + 2$
Simplify.
20. $(4a^{6} - 5a^{4} + 3a^{2} - a) \div (2a + 1)$
ANSWER:
 $2a^{5} - a^{4} - 2a^{3} + a^{2} + a - 1 + \frac{1}{2a + 1}$

21. **GEOMETRY** The volume of the rectangular prism is $3x^3 + 11x^2 - 114x - 80$ cubic units. What is the area of the base?



ANSWER: $x^{2} + 3x - 40$ units²

State the degree and leading coefficient of each polynomial in one variable. If it is not a polynomial in one variable, explain why.

$$22.\ 5x^6 - 3x^4 + x^3 - 9x^2 + 1$$

ANSWER: degree: 6; leading coefficient: 5 $23.\ 6xy^2 - xy + y^2$

ANSWER:

This is not a polynomial in one variable. It has two variables, *x* and *y*.

24.
$$12x^3 - 5x^4 + 6x^8 - 3x - 3$$

ANSWER: degree: 8; leading coefficient: 6

Find
$$p(-2)$$
 and $p(x + h)$ for each function.
25. $p(x) = x^2 + 2x - 3$
ANSWER:
 $p(-2) = -3; p(x + h) = x^2 + 2xh + h^2 + 2x + 2h - 3$

26.
$$p(x) = 3x^2 - x$$

ANSWER:
 $p(-2) = 14; p(x + h) = 3x^2 + 6xh + 3h^2 - x - h$
27. $p(x) = 3 - 5x^2 + x^3$

ANSWER:

$$p(-2) = -25; p(x + h) = 3 - 5x^{2} - 10xh - 5h^{2} + x^{3}$$

 $3hx^{2} + 3h^{2}x + h^{3}$

+

Complete each of the following.

a. Graph each function by making a table of values.

b. Determine the consecutive integer values of *x* between which each real zero is located.c. Estimate the *x*-coordinates at which the

relative maxima and minima occur.

28.
$$h(x) = x^3 - 4x^2 - 7x + 10$$

ANSWER:

a.



b. The zeros are at -2, 1, and 5. **c.** rel. max: $x \approx -0.69$; rel. min: $x \approx 3.36$

29.
$$g(x) = 4x^4 - 21x^2 + 5$$

ANSWER:



b. between -3 and -2, between -1 and 0, between 0 and 1, between 2 and 3 **c.** rel. max: $x \approx 0$; rel. min: $x \approx 1.62$ and $x \approx -1.62$

$$30.f(x) = x^3 - 3x^2 - 4x + 12$$

ANSWER:



b. zeros at -2, 2, and 3 **c.** rel. max: $x \approx -0.53$; rel. max: $x \approx 2.53$

31.
$$h(x) = 4x^3 - 6x^2 + 1$$

ANSWER:

a.



b. between -1 and 0, between 0 and 1, and between 1 and 2

c. rel. max: $x \approx 0$; rel. min: $x \approx 1$

$$32.\,p(x) = x^5 - x^4 + 1$$

ANSWER:







33. **BUSINESS** Milo tracked the monthly profits for his sports store business for the first six months of the year. They can be modeled by using the following six points: (1, 675), (2, 950), (3, 550), (4, 250), (5, 600), and (6, 400). How many turning points would the graph of a polynomial function through these points have? Describe them.

ANSWER:

2 relative maxima and 1 relative minima

Factor completely. If the polynomial is not factorable, write *prime*.

34. $a^4 - 16$

ANSWER:

 $(a-2)(a+2)(a^2+4)$

35. $x^3 + 6y^3$

ANSWER: prime

36. $54x^3y - 16y^4$

ANSWER:

$$2y(3x - 2y)(9x^2 + 6xy + 4y^2)$$

$$37. \ 6ay + 4by - 2cy + 3az + 2bz - cz$$

ANSWER: (2y+z)(3a+2b-c)

Solve each equation.

$$38. x^{3} + 2x^{2} - 35x = 0$$
ANSWER:

$$-7, 0, 5$$

$$39. 8x^{4} - 10x^{2} + 3 = 0$$
ANSWER:

$$\pm \frac{\sqrt{3}}{2}, \pm \frac{\sqrt{2}}{2}$$

40. **GEOMETRY** The volume of the prism is 315 cubic inches. Find the value of *x* and the length, height, and width.



ANSWER:

x = 6, length = 9 in., height = 5 in., width = 7 in.

Use synthetic substitution to find f(-2) and f(4) for each function.

41.
$$f(x) = x^2 - 3$$

ANSWER:
 $f(-2) = 1; f(4) = 13$
42. $f(x) = x^2 - 5x + 4$
ANSWER:
 $f(-2) = 18; f(4) = 0$
43. $f(x) = x^3 + 4x^2 - 3x + 2$
ANSWER:
 $f(-2) = 16; f(4) = 118$
44. $f(x) = 2x^4 - 3x^3 + 1$
ANSWER:
 $f(-2) = 57; f(4) = 321$

Given a polynomial and one of its factors, find the remaining factors of the polynomial.

45.
$$3x^{3} + 20x^{2} + 23x - 10; x + 5$$

ANSWER:
 $x + 2$ and $3x - 1$
46. $2x^{3} + 11x^{2} + 17x + 5; 2x + 5$
ANSWER:
 2 and $x^{2} + 3x + 1$
47. $x^{3} + 2x^{2} - 23x - 60; x - 5$
ANSWER:
 $x + 3, x + 4$
State the possible number of possible number

State the possible number of positive real zeros, negative real zeros, and imaginary zeros of each function.

 $48.f(x) = -2x^3 + 11x^2 - 3x + 2$

ANSWER:

positive real zeros: 3 or 1 negative real zeros: 0 imaginary zeros: 2 or 0

$$49.f(x) = -4x^4 - 2x^3 - 12x^2 - x - 23$$

ANSWER:

positive real zeros: 0 negative real zeros: 4, 2, or 0 imaginary zeros: 4, 2, or 0

$$50.f(x) = x^6 - 5x^3 + x^2 + x - 6$$

ANSWER:

positive real zeros: 3 or 1 negative real zeros: 1 imaginary zeros: 4 or 2

$$51.f(x) = -2x^5 + 4x^4 + x^2 - 3$$

ANSWER:

positive real zeros: 2 or 0 negative real zeros: 1 imaginary zeros: 4 or 2

$$52.f(x) = -2x^6 + 4x^4 + x^2 - 3x - 3$$

ANSWER:

positive real zeros: 2 or 0 negative real zeros: 2 or 0 imaginary zeros: 6, 4, or 2

Find all of the zeros of each function.

53.
$$f(x) = x^{3} + 4x^{2} + 3x - 2$$

ANSWER:
 $-2, -1 \pm \sqrt{2}$
54. $f(x) = 4x^{3} + 4x^{2} - x - 1$
ANSWER:
 $-1, -\frac{1}{2}, \frac{1}{2}$
55. $f(x) = x^{3} + 2x^{2} + 4x + 8$
ANSWER:
 $-2, \pm 2i$

56. **STORAGE** Melissa is building a storage box that is shaped like a rectangular prism. It will have a volume of 96 cubic feet. Using the diagram below, find the dimensions of the box.



ANSWER: width = 4 ft, length = 12 ft, height = 2 ft